

## NONLOCAL PROBLEM WITH INTEGRAL CONDITIONS FOR POLICALORIC EQUATION OF SECOND ORDER

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Let  $H(R \times R)$  be a class of certain functions,  $K_{L,M}$  be a class of quasi-polynomials in the form  $f(t, x) = \sum_{i=1}^n \sum_{j=1}^m R_{ij}(t, x) \exp[\alpha_i x + \beta_j t]$ , where  $R_{ij}(t, x)$  are given polynomials,  $\alpha_i \in M \subseteq C, \beta_j \in L \subseteq C$ , for  $\alpha_l \neq \alpha_k$  and  $\beta_l \neq \beta_k$ , for  $l \neq k$ , for  $k \in N, l \in N$ .

In the strip  $\Omega = \{(t, x) \in R^2 : t \in (0, T), x \in R\}$  we consider equation

$$\left[ \frac{\partial}{\partial t} - a \left( \frac{\partial}{\partial x} \right) \right]^2 U(t, x) = f(t, x), \quad (1)$$

satisfies nonlocal integral conditions

$$P_i \left( \frac{\partial}{\partial x} \right) \frac{\partial^k U(t, x)}{\partial t^k} \Big|_{t=0} + Q_i \left( \frac{\partial}{\partial x} \right) \frac{\partial^k U(t, x)}{\partial t^k} \Big|_{t=T} + \int_0^T t^k U(t, x) dt = 0, \quad (2)$$

for  $k=0,1$  where  $T > 0$ ,  $a_j \left( \frac{\partial}{\partial x} \right)$  are differential expressions, with analytical

symbol  $a(\lambda) \neq const$ ,  $p_i \left( \frac{\partial}{\partial x} \right), q_i \left( \frac{\partial}{\partial x} \right)$  are given differential polynomials, with analytical functions  $p_i(\lambda), q_i(\lambda)$ . Solution of the problem (1), (2), according to the differential-symbol method [1] exists and unique in the class of quasi-polynomials, which is represented in the form

$$U(t, x) = f \left( \frac{\partial}{\partial v}, \frac{\partial}{\partial \lambda} \right) \left\{ G(t, v, \lambda) \exp[\lambda x] \right\} \Big|_{v=\lambda=0},$$

where  $G(t, v, \lambda)$  is a solution of the problem

$$\left[ \frac{d}{dt} - a(\lambda) \right] G(t, v, \lambda) = \exp[vt],$$

$$\int_0^T G(t, v, \lambda) dt = 0, \quad \int_0^T tG(t, v, \lambda) dt = 0,$$

This result continues the research of work [2, 3].

1. *Kalenyuk P. I. Nytrebych Z. M.* Generalized Scheme of Separation of Variables. Differential-Symbol Method. – Publishing House of Lviv Polytechnic National University, 2002. – 292 p. (in Ukrainian).
2. *Kalenyuk P. I. Nytrebych Z. M. Kohut I. V. Kuduk G.* Problem for nonhomogeneous second order evolution equation with homogeneous integral conditions // *Math. Methods and Phys.-Mech. Fields.* – 2015. – Vol. 58, No 1. – P. 7-19.
3. *Kalenyuk P. I. Nytrebych Z. M. Kohut I. V. Kuduk G, Pukach P. Ya.* Problem with homogeneous integral condition for nonhomogeneous evolution equation.// *Journal of National Univeristy «Lvivska Politechnika».* Phys. and Math. sciences. – 2014. – No. 804. – P. 16-20.

### **НЕЛОКАЛЬНА ЗАДАЧА З ІНТЕГРАЛЬНИМИ УМОВАМИ ДЛЯ ПОЛІКАЛОРИЧНОГО РІВНЯННЯ ДРУГОГО ПОРЯДКУ**

*За допомогою диференціально-символьного методу побудовано розв'язок нелокальної задачі з інтегральними умовами для полікалоричного рівняння другого порядку в класі квазімногочленів, і доведено його єдиність.*