

Antonova T. M., Hoyenko N. P.

**APPROXIMATION OF RATIO OF LAURICELLA FUNCTIONS F_D
BY NÖRLUND'S BRANCHED CONTINUED FRACTION
IN COMPLEX DOMAIN**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 7-15. – Ref.: 13 names. – Ukr.

The convergence of Nörlund's branched continued fraction, that is the expansion of ratio of Lauricella hypergeometric functions $F_D^N(a, b_1, b_2, \dots, b_N; c; z_1, z_2, \dots, z_N)$ in the domain $\{\operatorname{Re} z_k < 1/2, k=1, N\}$, when parameters hold $a \geq 0, b_i \geq 0, i = 1, N, 2c \geq a + b_1 + b_2 + \dots + b_N + 1$, is investigated.

Dmytryshyn M. I.

**INTERPOLATION OF SPECTRAL SUBSPACES
OF TRICOMI DIFFERENTIAL OPERATORS**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 16-21. – Ref.: 8 names. – Ukr.

The interpolation properties of Tricomi differential operators are established. The spectral decompositions of such operators are given.

Vozna S. M.

ON CONVERGENCE OF CONTINUED J -FRACTION

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 22-29. – Ref.: 11 names. – Ukr.

The connection between a continued J -fraction and associated continued fraction, obtained from some interpolation problem, has been shown. The convergence of continued J -fraction with partial quotients of the form $\frac{-c_n^2}{ib_n + z}$ has been investigated.

Zagorodnyuk A. V., Chernega I. V.

**SYMMETRIES OF ANALYTIC FUNCTION SPACES
ON BANACH SPACES**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 30-34. – Ref.: 10 names. – Ukr.

Algebras of analytic functions on Banach space, which are symmetric with respect to some semi-group of isometric operators, are investigated. Operator of symmetrization, which is a homomorphism of algebras, is constructed.

Yeleyko Ya. I., Zhernovy Yu. V.

**ASYMPTOTIC PROPERTIES OF RANDOM EVOLUTIONS
CONSTRUCTED ON THE BASIS OF SOLUTIONS FOR SYSTEMS
OF ORDINARY DIFFERENTIAL EQUATIONS**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 35-43. – Ref.: 8 names. – Ukr.

The work describes as random evolutions on the trajectories of semi-markovian process random wanderings of arbitrary nature system, parameters of which are variable in time onto a finite set of conditions and each condition is described by solutions of Cauchy problem for a system of ordinary differential equations. On the basis of ergodic Skorochod theorem for the processes with markovian interference of the case, the asymptotics of additive function at $t \rightarrow \infty$, which determines the mean value of random evolution in time, is found. Random evolution with finite number of opportunities (sub-conditions) for each condition of markovian process is investigated. Evolution for mathematical model of development of populations of biological species is constructed.

Lozynska V. Ya., M'yaus O. M.

**DISTRIBUTIONS OF EXPONENTIAL TYPE
AND FUNCTIONAL CALCULUS**

ISSN 0130-9420. *Mathematical methods and physico-mechanical fields.* – 2004. – 47, No. 2. – P. 44-49. – Ref.: 9 names. – Ukr.

Some properties of operator calculus for generators of strongly continuous groups of linear operators on arbitrary Banach spaces are described.

O. Lyzun

ENTIRE FUNCTIONS WITH PRESCRIBED GROWTH

ISSN 0130-9420. *Mathematical methods and physico-mechanical fields.* – 2004. – 47, No. 2. – P. 50-59. – Ref.: 7 names. – Engl.

Entire function f with prescribed growth of its main characteristics is constructed in the form of certain infinite product such that

$$N(r, f) \square T(r, f) \square \log m_q(r, f) \square \log M(r, f) \square m_2(r, \log |f|) \square \lambda(r), \quad r \rightarrow \infty,$$

where m_q are q -integral means and $\lambda(r)$ is a positive, continuous, increasing to $+\infty$, and convex with respect to $\log r$ function.

O. V. Verbitsky

ON DUAL VERSION OF WEISFEILER – LEHMAN ALGORITHM

ISSN 0130-9420. *Mathematical methods and physico-mechanical fields.* – 2004. – 47, No. 2. – P. 60-64. – Ref.: 5 names. – Engl.

We study a simplified variant of the Weisfeiler – Lehman graph canonization algorithm that corresponds to the fragment of the first order logic with bounded number of variables precisely in the same way as the standard variant corresponds to this fragment, enriched with counting quantifiers. We propose a natural dual version of the color refinement subroutine and prove that the dual algorithm has optimum dimension by one exceeding that of the standard algorithm.

Maslyuchenko V. K., Maslyuchenko O. V., Mykhaylyuk V. V.

PARACOMPACTNESS AND LEBESGUE CLASSIFICATION

ISSN 0130-9420. *Mathematical methods and physico-mechanical fields.* – 2004. – 47, No. 2. – P. 65-72. – Ref.: 12 names. – Ukr.

Generalization of the known Kuratowski – Montgomery theorem about the Lebesgue classification of separately continuous mappings is proposed.

Mytrofanov M. A.

DISTRIBUTIONS ON CUBE IN HILBERT SPACE

ISSN 0130-9420. *Mathematical methods and physico-mechanical fields.* – 2004. – 47, No. 2. – P. 73-77. – Ref.: 10 names. – Ukr.

We construct a space of distributions on a cube in Hilbert space. We define the operations of differentiation and multiplication on this space.

Novosad Z. G.

**COMPOSITION OPERATORS ON SPACES OF ANALYTIC
FUNCTIONS ON HILBERT SPACE**

ISSN 0130-9420. *Mathematical methods and physico-mechanical fields.* – 2004. – 47, No. 2. – P. 78-83. – Ref.: 10 names. – Ukr.

The spectral properties of composition operators on Hilbert space of analytic functions, which are defined on the unit Hilbert ball, are investigated. The spectral theorem for such operators is proved.

Pipa G. M., Storozh O. G.

**SEMI-SMOOTH RESTRICTIONS OF POSITIVELY DEFINED OPERATOR
AND THEIR PROPER EXTENSIONS**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 84-89. – Ref.: 13 names. – Ukr.

Let L_0 be a closed symmetric positively defined operator in Hilbert space and L_{\min} – its restrictions onto the kernel of auxiliary linear mapping, defined on the energetic space of L_0 . In terms of abstract boundary conditions various extensions (self-adjoint, maximal non-negative etc.) of L_{\min} are described.

Skaskiv O. B., Trusevych O. M., Kyrychynska I. B.

**ON A SUM AND MAXIMUM TERM OF SERIES SIMILAR
TO TAYLOR – DIRICHLET SERIES**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 90-94. – Ref.: 7 names. – Ukr.

We establish conditions, under which for positive series of the form $F(x) = \sum_{n=0}^{+\infty} a_n e^{\lambda_n x + \tau(x)\beta_n}$ the relation $F(x) = (1 + o(1)) \max \{ a_n e^{\lambda_n x + \tau(x)\beta_n} : n \geq 0 \}$ holds with $x \rightarrow +\infty$ outside some exceptional set, where τ is a positive on $[0, +\infty)$ function, λ_n and β_n are positive sequences.

Solomko A. V., Lopushansky O. V., Sharin S. V.

**ON TOPOLOGICAL ISOMORPHISM OF DISTRIBUTION ALGEBRA
WITH SUPPORTS IN CONE TO COMMUTANT OF SHIFT SEMIGROUP**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 95-99. – Ref.: 4 names. – Ukr.

The properties of dual pair $\langle D'_\Gamma, D_\Gamma \rangle$, associated with classical convolution algebra of Schwartz distributions with supports in the cone $\Gamma \subset \mathbf{R}^n$, are investigated. The operation of cross-correlation with respect to constructed duality is defined. The theorem about topological isomorphism of the convolution algebra D'_Γ to commutant of the (C_0) -semi-group in algebra $L(D_\Gamma)$ on the corresponding space of test functions is proved.

Hentosh O. E.

**HAMILTONIAN REDUCTION OF NEUMANN TYPE
FOR DAVEY – STEWARTSON SYSTEM**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 100-107. – Ref.: 11 names. – Ukr.

For the Davey – Stewartson (2+1)-dimensional nonlinear dynamic system, possessing the triple matrix Lax representation, the method of reducing upon its non-local finite-dimensional solution subspace is developed.

Guzil' N. I., Lavrenyuk S. P.

**PROBLEM WITHOUT INITIAL DATA
FOR HYPERBOLIC SYSTEM OF THE FIRST ORDER**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 108-115. – Ref.: 11 names. – Ukr.

In the article the problem without initial data for hyperbolic system of the form

$$u_t + \sum_{i=1}^l A_i(x, t) u_{x_i} + C(x, t) u + g(t, u) = f(x, t)$$

in the bounded on the variable x domain is considered. Some sufficient conditions of existence and uniqueness of solution independently of its behavior, when $t \rightarrow -\infty$, are obtained.

Pukal'sky I. D.

**PROBLEM WITH DIRECTIONAL DERIVATIVE FOR SINGULAR
ELLIPTIC EQUATIONS**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 116-123. – Ref.: 4 names. – Ukr.

The existence and uniqueness of the problem with directional derivative for singular non-uniformly elliptic equations without limitation on the power order of coefficient degeneration have been proved in the spaces of classic functions with the power weight. Estimate of the solution to the problem in the corresponding spaces has been found.

Bozhenko B. L., Nagirny T. S.

**ON NUMERICAL SOLUTION OF VARIATIONAL PROBLEMS
OF LOCAL GRADIENT MECHANICS USING
MOVING LEAST-SQUARE APPROXIMATIONS**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 124-128. – Ref.: 10 names. – Ukr.

The basic relations of local gradient thermo-elasticity are formulated. The meshless method for solution and investigation of the corresponding problems of mathematical physics, using moving least-squares approximations, is proposed.

Danoyan Z. N.

**INVESTIGATION OF ROOTS OF CHARACTERISTIC
EQUATION OF PLANE MAGNETOELASTIC WAVES
FOR PERFECTLY-CONDUCTING ANISOTROPIC MEDIA**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 129-137. – Ref.: 9 names. – Russian.

On the basis of the Smirnov – Sobolev's method, the functional-invariant solutions of magnetoelasticity bidimensional equations for perfectly-conducting anisotropic media, representing plane magnetoelastic waves, are studied. The behavior of roots of corresponding characteristic equation, depending upon the values of elastic constants and magnitude of external magnetic field, are investigated in details. It is shown, that the roots of characteristic equation, depending on the above stated parameters, can be of two types: either each root corresponds to the unique interval reality, or one of them is real in two non-crossing intervals, and another is real in one interval.

Kryven' V. A., Yavorska V. I.

**PLASTIC ZONES AT SHEAR NEAR RECTANGULAR AND ROUNDED
CUTS OF CONSTANT WIDTH**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 138-144. – Ref.: 6 names. – Ukr.

Stressed-strained state of ideal elastico-plastic body with semi-infinite rectangular and rounded cuts of constant width under the conditions of anti-plane strain is investigated. Analytical solutions of the problems are found, the plastic zone development is investigated. It is shown that the zone shape can be approximated by solution of elastico-plastic problem for a semi-infinite crack, when the maximum size of plastic zone several times exceeds the cut width.

Kondrat V. F.

**ON STUDIES OF VIBRO-EVOLUTIONARY PHENOMENA
IN NONLINEAR MECHANICS OF CONJUGATED FIELDS**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 145-150. – Ref.: 22 names. – Ukr.

We propose a method to obtain an approximate solution to nonlinear problem of mechanics of conjugated fields as applied to vibro-evolutionary phenomena.

Ostudin B. A., Romanenko A. V.

**MATHEMATICAL MODELING OF HEAVY-CURRENT BEAM
IN SELF-CONSISTENT 3D-FIELD**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 151-162. – Ref.:

19 names. – Ukr.

Basing on the integral equation method, an algorithm for solution of three-dimensional stationary self-consistent problem is constructed. The numerical-analytical approach has been used to define the potential and strength of electric field. The proposed algorithm has been verified on the plane-parallel diode with unlimited cathode capability. Generalization for the case of cylindrical charged surfaces has been considered.

Pyanylo Ya. D., Popovych V. S., Pyanylo A. Ya.

**ITERATIVE SCHEME FOR SOLUTION OF NONLINEAR BOUNDARY-VALUE PROBLEMS
OF NON-STATIONARY HEAT CONDUCTIVITY TYPE**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 163-167. – Ref.: 10 names. – Ukr.

The iterative scheme for solution of nonlinear partial differential equations of heat conductivity type is proposed. Convergence of the constructed iterative scheme is proved.

Sarkisyan S. V., Pogosyan A. S.

**ABOUT MAGNETOELASTIC VIBRATIONS OF TRANSVERSALLY ISOTROPIC
PLATES ACCORDING TO SHEAR STRAIN**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 168-172. – Ref.: 8 names. – Russian.

The problem on vibration of transversally isotropic electroconductive plate is investigated in the presence of constant magnetic field, involving cross shear strain. For change of the plate thickness components of electromagnetic field two cases are considered.

Chernukha O. Yu.

**ADMIXTURE DIFFUSION IN RANDOMLY
NON-HOMOGENEOUS FIBROUS LAYER**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 173-180. – Ref.: 13 names. – Ukr.

Admixture diffusion has been considered in a layer, formed of two phases being different by diffusive properties: matrix and fibrous inclusions, located randomly. The conditions of non-ideal mass contact are imposed on the interphases. The contact initial boundary-value problem is reduced to the non-linear integro-differential equation, which has been solved by the method of successive iterations. Convergence of Neumann series has been proved for this case. The approximate formula is found for concentration, averaged over ensemble of phase configurations.

Zabolotsky M. V., Sheremeta Z. M.

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 181-185. – Ref.: 7 names. – Ukr.

**ON INDEX BOUNDEDNESS OF ENTIRE SOLUTION
TO ONE DIFFERENTIAL EQUATION**

For $l(x) \equiv \text{const} > 1$, the l -index boundedness of entire solution to the differential equation $z^2 w'' + (\beta_0 z^2 + \beta_1 z) w' + (\gamma_0 z^2 + \gamma_1 z + \gamma_2) w = 0$ is investigated.

Sheremeta Z. M., Sheremeta M. M.

**CONVEXITY OF ENTIRE SOLUTIONS
OF ONE DIFFERENTIAL EQUATION**

ISSN 0130-9420. Mathematical methods and physico-mechanical fields. – 2004. – 47, No. 2. – P. 186-191. – Ref.: 7 names. – Ukr.

Conditions on constant coefficients of differential equation $z^2 w'' + (\beta_0 z^2 + \beta_1 z) w' + (\gamma_0 z^2 + \gamma_1 z + \gamma_2) w = 0$, under which the entire solution f of equation and all its derivatives f', f'', \dots are convex in the unit disk, are investigated.